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Torseforming Curvature and Ricci Tensor in a Trans- Sasakian Manifold Shankar lal Departmnt of Mathematics HNB Garhwal University SRT Campus, Badshahi Thaul

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Abstract. The aim of the present paper, I have studied Torseforming Curvature and Ricci Tensor in a Trans-Sasakian Manifold. The sectional curvature of a plane section of such a manifold containing U is a constant, saysC. He divided these manifolds into three cases: (1) homogeneous normal contact Riemannian manifold with C >0, (2) global Riemannian products of a line or a circle with a manifold of constants holomorphic sectional curvature if C = 0 and (3) a warped product space $R_{Xf} C^{\infty}$ if C>0.

I know that the manifolds belonging to class (1) is characterized by admitting a Sasakian structure. I have also obtained necessary and sufficient condition that trans-Sasakian manifold is flat. Here we proved that the trans-Sasakian manifold satisfying the condition R(X, Y)S = 0 and torseforming trans-Sasakian manifolds in a curvature and Ricci

tensor under these condition $\varphi \operatorname{grad} \alpha = \operatorname{grad} \beta$, is a consircular tensor.

Key Words: trans-Sasakian manifold, torseforming curvature and Ricci tensor, concircular tensor.

Introduction. The purpose of the present paper is to define and study the torseforming Curvature and Ricci tensor in a trans-Sasakian manifold. In section 1 we review and collect some necessary results. In section 2 I define trans-Sasakian manifolds satisfying the condition R(X, Y) = 0. In section 3 I have also define torseforming trans-Sasakian manifolds. The contact manifolds are n = 2m + 1 dimensional manifolds with specified contact structure. I can obtain different structure like Sasakian, Quasi Sasakian, Kenmotsu and trans-Sasakian by providing additional conditions. The geometry of the manifolds is extensively studied trans-Sasakian manifold and invariant sub-manifolds of a conformal K-contact Riemannian manifold by [3] to [2]. Now the torseforming vector field in a Riemannian manifold has been introduced by K. Yano in 1944 [10].

In this paper I have also defined a conformally contact Riemannian manifold and established some of its properties and another meaningful results.

1. Preliminaries. Let us consider an n = 2m + 1 dimension real differentiable manifold with an almost contact metric structure (F,U,u, g) on which there are defined a tensor field of type (1,1), a vector field U and 1-form u satisfying for every vector field X

(1 1) (a)	$\mathbf{V} = \mathbf{I}$, $\mathbf{v} = \mathbf{I}$	(h)	$\mathbf{F}(\mathbf{V}) = \mathbf{V}$
(1.1) (a)	$\mathbf{X} = \mathbf{I} + \mathbf{u} \mathbf{U},$	(D)	$\mathbf{F}(\mathbf{X}) = \mathbf{X}$
(=-=) ()	,	()	- ()

(c)	$\mathbf{u}(\mathbf{U}) = \mathbf{-}, 1$	(d)	$\mathbf{u}(\mathbf{X}) = 0$	(e)	$\mathbf{U} = 0$
				· · ·	

and rank $\varphi = n = 2m + 1$.

Where I is the identity endomorphism of the tangent bundle of M^n (1.2) (a) $g(\overline{X}, \overline{Y}) = -g(X, Y) - u(X)u(Y)$,

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(b) g(X,Y) = -g(X,Y),
 (c) g(X,U) = u(X) for all X,Y TM.

An almost contact metric structure (F,U,u,g) on M^n is called a trans-Sasakian structure, then consider the manifold $(M^n \cdot R, J, g_1)$ and denoted by $(X, f - \frac{d}{dt})$ a vector field of $M^n \cdot R$, where X is a tangent to M^n , t is the field of R and f is a differentiable function on $M^n \cdot R$. An almost complex structure J on this manifold is defined as

(1.3) J X, f
$$\frac{d}{dt} = X - fU,u(X)$$
 $\frac{d}{dt}$

for all vector field X on M^n and smooth function a on $M^n \cdot R$ and g_1 is the product metric on $M^n \cdot R$. It is known that $(M^n \cdot R, J, g_1)$ is an almost Hermitian manifold [11], where g_1 denote the product metric given by

(1.4)
$$g_1 \quad X, f \quad \frac{d}{dt} \quad Y, h \quad \frac{d}{dt} = g(X, Y) + fh$$

I now recall the following important result due to Lotta by [1].

Let Mⁿ be a slant sub-manifold of an almost contact metric manifold Mⁿ with slant angle $\theta \neq \frac{\pi}{2}$, then we have

$$2 n = 2m + 1 is odd \quad U is tangent to M.$$

This is may be expressed by the condition [7]

(1.5)
$$\overline{XY} = \alpha\{g(X,Y)U - u(Y)X\} + \beta\{g(\overline{X},Y)U - u(Y)X\},$$

for some smooth functions α and β on Mⁿ and we say that trans-Sasakian structure is of type (α , β). From (1.5) it follows that

(1.6) (a)
$$_{X}U = -\alpha (\overline{X}) + \beta \{X - u(X)U\}$$

(b) $(_{X}u)Y = -\alpha g(\overline{X}, Y) + \beta g(\overline{X}, \overline{Y})$

I note that the trans-Sasakian structures of type (0,0) are cosymplectic trans-Sasakian structures of type $(0, \beta)$ are β -Kenmotsu and trans-Sasakian structures of type (a)0 are α -Sasakian. Thus, in trans-Sasakian structures of type (0,0), the equations (1.5) and (1.6) reduce to

(1.7)
$$x = 0, \quad xU = 0.$$

For β – Kenmotsu structure (1.5) and (1.6) reduce to

(1.8) (a)
$$X Y = \beta \{g(X, Y)U - u(Y)X\}$$

(b) $_{\mathbf{X}}\mathbf{U} = \boldsymbol{\beta}\{\mathbf{X} - \mathbf{u}(\mathbf{X})\mathbf{U}\},\$

while for α – Sasakian. Structure, we have

(1.9) (a)
$$X Y = a\{g(X, Y)U - u(Y)X\},\$$

(b) $_{\mathbf{X}}\mathbf{U} = -\boldsymbol{\alpha}(\mathbf{X})$,

If $\alpha = 1$, $\alpha -$ Sasakian. Structure reduce to Sasakian on trans-Sasakian manifolds, we have the following result.

(1.10)
$$\mathbf{R}(\mathbf{X},\mathbf{Y})\mathbf{U} = (\boldsymbol{\alpha}^2 - \boldsymbol{\beta}^2)\{\mathbf{u}(\mathbf{Y})\mathbf{X} - \mathbf{u}(\mathbf{X})\mathbf{Y}\} + 2\boldsymbol{\alpha}\boldsymbol{\beta}\{\mathbf{u}(\mathbf{Y})(\mathbf{X}) - \mathbf{u}(\mathbf{X})\mathbf{Y}\} + \mathbf{Y}\boldsymbol{\alpha}(\mathbf{X}) - \mathbf{X}\boldsymbol{\alpha}(\mathbf{Y}) + \mathbf{Y}\boldsymbol{\beta}(\mathbf{X}) - \mathbf{X}\boldsymbol{\beta}(\mathbf{Y}),$$

(1.11)
$$R(U, X) = (\alpha^2 - \beta^2 - U\beta) \{u(X)U - X\},$$

(1.12) $2\alpha\beta + U\alpha = 0$,

(1.13)
$$S(X, U) = \{2m(\alpha^2 - \beta^2) - U\beta\}u(X) - (2m - 1)X\beta - (X)\alpha,$$

(1.14)
$$QU = \{2m(\alpha^2 - \beta^2) - U\beta\}U - (2m - 1)grad\beta + grad\alpha,$$

When φ grad $\alpha = (2m - 1)$ grad β , from equations (113), and (1.14) reduce to

(1.15) S(X,U) - 2m(
$$a^2 - \beta^2$$
)u(X),

(1.16)
$$QU = 2m(\alpha^2 - \beta^2)U$$
.

Also under the above condition $\varphi \operatorname{grad} \alpha = (2m - 1)\operatorname{grad} \beta$ the expression for Ricci tensor and scalar curvature in a trans-Sasakian manifold are given respectively by

(1.17)
$$S(X,Y) = \frac{\Gamma}{2} - (\alpha^2 - \beta^2) g(X,Y) - \frac{\Gamma}{2} - 3(\alpha^2 - \beta^2) u(X) u(Y)$$

and

(1.18)
$$R(X,Y)Z = \frac{r}{2} - 2(\alpha^{2} - \beta^{2}) \left[g(Y,Z)X - g(X,Z)Y \right] - \frac{r}{2} - 3(\alpha^{2} - \beta^{2}) \left[g(Y,Z)u(X)U - g(X,Z)u(Y)U \right] - \frac{r}{2} - 3(\alpha^{2} - \beta^{2}) \left[u(Y)u(Z)X - u(X)u(Z)Y \right],$$

A vector field ρ defined by $g(X, \rho) = w(X)$ for any vector field X is said to be a torseforming curvature and Ricci tensor

(1.19) $(X w)Y = kg(X,Y) + \pi(X)w(Y)$, where k is a non-zero scalar and π is a non-zero 1-form.

2. Curvature and Ricci tensor in a trans-Sasakian manifold satisfying the condition R(X, Y) = 0.

Let us consider a trans-Sasakian manifold Mⁿ which satisfying the condition (2.1) R(X,Y) = 0. From (2.1), (2.2) S(R(X,Y)U,u) + S(U, R(X,Y)u) = 0. Putting X = U and using (1.10) and (1.1), we have (2.3) $R(U,Y)U = (\alpha^2 - \beta^2) \{u(Y)U + Y\} + 2\alpha\beta \overline{Y} - U\alpha \overline{(Y)} - U\beta \overline{(Y)}$ using (111) in (2.3), we have (2.4) $(\alpha^2 - \beta^2) \{u(Y)U + Y - u(X)U + X\} + U\beta \{u(X)U - X + Y + 2\alpha\beta \overline{Y} - U\alpha \overline{(Y)} = 0$.

Let $\{e_i\}, i = 1 \ 2 \ 3$n be an orthonormal basis of the tangent space at each point of the manifold M n . Then putting $\,X=Y=e_i\,$ in (2.4) and taking summation for 1< i < n , we obtain

(2.5) $2(\alpha^2 - \beta^2)\mathbf{e}_i + \mathbf{e}_i\beta \{\mathbf{u}(\mathbf{e}_i)\mathbf{e}_i - \mathbf{e}_i + \mathbf{e}_i + 2\alpha\beta\mathbf{e}_i - \alpha\mathbf{e}_i = 0$ and using (1.12), we have

$$2\alpha\beta + e_i\alpha = 0$$

$$2\beta + e_i = 0$$

$$e_i = -\frac{\beta}{2},$$

Substituting the value of e_i in the above equation (2.5), we get

(2.6)
$$-\beta \alpha^2 - 2\alpha \beta^2 - \frac{\beta^2}{2} + \frac{3\beta^3}{4} - \frac{\beta_4}{2} - \alpha \left\| \frac{\beta}{2} \right\| = 0$$

3. Torseforming Curvature and Ricci tensor in a trans-Sasakian manifold

Consider a unit torseforming vector field ρ in a tensor form corresponding to a vector field ρ . Suppose $g(X, \rho) = T(X)$, then the metric tensor is

(3.1)
$$T(X) = \frac{w(X)}{\sqrt{w(\rho)}}$$

From (1.19) divided into $\frac{1}{\sqrt{w(\rho)}}$ both sides, we get

(3.2)
$$\frac{(\mathbf{X} \mathbf{W})\mathbf{Y}}{\sqrt{\mathbf{W}(\boldsymbol{\rho})}} = \frac{\mathbf{k}}{\sqrt{\mathbf{W}(\boldsymbol{\rho})}} \mathbf{g}(\mathbf{X},\mathbf{Y}) + \frac{\pi}{\sqrt{\mathbf{W}(\boldsymbol{\rho})}} \mathbf{W}(\mathbf{Y}),$$

using equation (3.1) in the equation, we obtain

(3.3)
$$(X T)Y = \frac{k}{\sqrt{w(\rho)}} g(X,Y) + \pi(X)T(Y) ,$$

Putting $Y = \overline{\rho}$ in (3.3), we obtain

(3.4)
$$(\mathbf{X} \mathbf{T})\overline{\rho} = \frac{\mathbf{k}}{\sqrt{\mathbf{w}(\rho)}} \mathbf{g}(\mathbf{X}, \overline{\rho}) + \pi(\mathbf{X})\mathbf{T}(\overline{\rho})$$

As $T(\overline{\rho}) = g(\overline{\rho}, \overline{\rho}) = 1$ is a unit vector then the equation (3.4) reduce to

(3.5)
$$(\mathbf{X} \mathbf{T})\overline{\rho} = \frac{\mathbf{k}}{\sqrt{\mathbf{w}(\rho)}} \mathbf{g}(\mathbf{X}, \overline{\rho}) + \pi(\mathbf{X})$$

and hence equation (3.3) can be written as in the form

(3.6)
$$(X T)(\rho) = \frac{k}{\sqrt{w(\rho)}} g(X,Y) + T(X)T(Y).$$

T is closed.

Using covariant differential of (3.6) and using Ricci identity, we get (3.7) $- T(R(X,Y)Z) = X \qquad [g(Y, Z) - T(Y)T(Z)] - Y \qquad [g(X, Z - T(X)T(Z)]$

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$$\sqrt{w(\rho)} \qquad \sqrt{w(\rho)} + \frac{k^2}{\sqrt{w(\rho)}} [g(Y, Z)T(X) - g(X,Z)T(Y)].$$

Using equations (1.18) and (3.1) in equation (3.7), we have

(3.8)
$$-w = \frac{r}{2} - 2(a^2 - \beta^2) \left[g(Y, Z)X - g(X, Z)Y \right] - \frac{r}{2} - 3(a^2 - \beta^2) \left[g(Y, Z)u(X)U - g(X, Z)u(Y)U \right] - \frac{r}{2} - 3(a^2 - \beta^2) \left[u(Y)u(Z)X - u(X)u(Z)Y \right]$$

$$\frac{r}{2} - 3(a^2 - \beta^2) \left[u(Y)u(Z)X - u(X)(Z)Y \right] = kX g(Y, Z) - \frac{w(Y)w(Z)}{w(\rho)}$$
$$-kY = g(X, Z) - \frac{w(X)w(Z)}{w(\rho)} + k^2 - g(Y, Z) - \frac{w(X)}{\sqrt{w(\rho)}} - g(X, Z) - \frac{w(Y)}{\sqrt{w(\rho)}}$$

Putting $Z = \rho$ and using $g(X, \rho) = T(X)$ and equation (3.1), we have

(3.9)
$$\mathbf{w} \quad \frac{\mathbf{r}}{2} - 2(\alpha^{2} - \beta^{2}) \left[g(\mathbf{Y}, \rho) \mathbf{X} - g(\mathbf{X}, \rho) \mathbf{Y} \right] - \frac{\mathbf{r}}{2} - 3(\alpha^{2} - \beta^{2}) \left[g(\mathbf{Y}, \rho) \mathbf{u}(\mathbf{X}) \mathbf{U} - g(\mathbf{X}, \rho) \mathbf{u}(\mathbf{Y}) \mathbf{U} \right] - \frac{\mathbf{r}}{2} - 3(\alpha^{2} - \beta^{2}) \left[u(\mathbf{Y}) u(\rho) \mathbf{X} - u(\overline{\mathbf{X}}) u(\rho) \mathbf{Y} \right] - \frac{\mathbf{r}}{2} - 3(\alpha^{2} - \beta^{2}) \left[u(\mathbf{Y}) u(\rho) \mathbf{X} - u(\overline{\mathbf{X}}) u(\rho) \mathbf{Y} \right] - \frac{\mathbf{r}}{2} - 3(\alpha^{2} - \beta^{2}) \left[u(\mathbf{Y}) u(\rho) \mathbf{X} - u(\overline{\mathbf{X}}) u(\rho) \mathbf{Y} \right] - \frac{\mathbf{r}}{2} - 3(\alpha^{2} - \beta^{2}) \left[u(\mathbf{Y}) u(\rho) \mathbf{X} - u(\overline{\mathbf{X}}) u(\rho) \mathbf{Y} \right] + \mathbf{k} \mathbf{X} g(\mathbf{Y}, \rho) - \frac{\mathbf{r}}{2} - \frac{\mathbf{w}(\mathbf{Y}) \mathbf{w}(\overline{\rho})}{\mathbf{w}(\rho)}$$

$$-kY \quad g(X,\rho) = \frac{W(X)W(\rho)}{W(\rho)} + k^{2} \quad g(Y,\rho) = \frac{W(X)}{\sqrt{W(\rho)}} - g(X,\rho) = \frac{W(Y)}{\sqrt{W(\rho)}} = 0,$$

$$(3.10) \quad \frac{\Gamma}{2} - 2(\sigma - \beta)^{2} = \frac{2}{[W(Y)X - W(X)Y]} \qquad \qquad \frac{\Gamma}{2} - 3(\sigma - \beta)[W(Y)U(X)U - W(X)U(Y)U]$$

$$+ \left[1 - W(\rho)\right] [kXW(Y) - kYW(X)] = 0,$$
Putting $X = \rho$ in equation (3.10) and $T(\rho) = g(\rho, \rho) = 1$, we have
$$(3.11 \quad \frac{\Gamma}{2} - 2(\sigma^{2} - \beta^{2}) \quad [X - Y] - \frac{\Gamma}{2} - 3(\sigma^{2} - \beta^{2}) \quad [u(X)U - u(Y)U] + (1 - W(\rho))[kX - kY] = 0.$$

Thus, we have the following.

Lemma 1. If a trans-Sasakian manifold admits a torseforming vector field then the following cases occur

(3.12) $u(Y) - u(\rho)T(Y) = 0$,

(3.13) $g(Y,U) \sqrt{w(\rho)} - w(X)w(Y) = 0.$

I first consider the case where (3.12) holds well. From (3.12), we get

$$u(\mathbf{Y}) = U(\boldsymbol{\rho})\mathbf{T}(\mathbf{Y})$$

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Now Y = U implies $1 = \left(\mathbf{u}((\overline{\boldsymbol{\rho}}))^2 \right)^2$ and thus $u(\overline{\rho}) = \pm 1.$ So (3.14) $u(Y) = \pm T(Y)$, using (3.14) in (1.6) in view of (3.6), we have (3.15) $- \alpha g(X,Y) + \beta g(X,Y) - T(X)T(Y) = \pm \underline{k} [g(X,Y) - T(X)T(Y)].$ (3.16)

$$\sqrt{w(\rho)}$$

Lemma 2. The equation (3.12) implies that the vector field $\overline{\rho}$ is a concircular vector field

d. I next assume the case (3.13), then

 $u(Y) - u(\overline{\rho})T(Y) \neq 0$. (3.17)

From (3.7), we obtain

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$$\frac{k}{\sqrt{w(\rho)}} - \frac{k}{\sqrt{w(\rho)}} - \frac{2k^2}{W(\rho)} T(X),$$

(3.19)
$$-wQ(X) = kX + \frac{\overline{\rho}}{\sqrt{w(\rho)}} + \frac{2k}{w(\rho)} - kw(X).$$

Putting X = U and using (1.16), we have

(3.20)
$$2\mathbf{m}(\alpha^2 - \beta^2) = \mathbf{k} + \frac{\rho}{\sqrt{\mathbf{w}(\rho)}} + \frac{2\mathbf{k}}{\mathbf{w}(\rho)} \mathbf{k}\mathbf{w}.$$

Putting X = U in equation (3.10), in virtue of (3.20) and T(U) = $u(\rho)$, we get

(3.21)

(321)
$$\frac{\mathbf{r}}{2} \cdot \frac{\mathbf{k}}{\mathbf{m}} \cdot \frac{\mathbf{kw}}{\mathbf{m}} \cdot \frac{\overline{\rho}}{\sqrt{\mathbf{w}(\rho)}} \cdot \frac{2\mathbf{k}}{\mathbf{w}(\rho)} \left[\mathbf{wU}(\mathbf{X}) - \mathbf{w}(\mathbf{X})\mathbf{U} \right]$$
$$- \mathbf{w}(\mathbf{X})\mathbf{U} = \frac{\mathbf{r}}{2} \cdot \frac{3\mathbf{k}}{2\mathbf{m}} \cdot \frac{3\mathbf{kw}}{2\mathbf{m}} \cdot \frac{\overline{\rho}}{\sqrt{\mathbf{w}(\rho)}} \cdot \frac{2\mathbf{k}}{\mathbf{w}(\rho)}$$
$$+ \left[1 - \mathbf{w}(\overline{\rho}) \right] \left[\mathbf{kXw}(\mathbf{U} - \mathbf{kUw}(\mathbf{X}) = \mathbf{0} \right].$$
From (3.5) it follows that

(3.22)
$$Y(X T)\rho = Y \frac{k}{\sqrt{w(\rho)}} g(X, \rho) + \frac{k}{\sqrt{w(\rho)}} [Yg(X, \rho)] + Y[\pi(X)],$$

since T is closed, π is also closed.

Then we have

Lemma 3. The above equations imply that the Curvature and Ricci tensor of vector field ρ is

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a concircular tensor. Thus from Lemma 2 and Lemma 3, we have state following. Theorem 3.1 A torseforming tensor in a trans-Sasakian manifold is a concircular tensor field.

From (1.6) it follows that in a trans-Sasakian manifoldU is a torseforming tensor field. Theorem 3.1, I can state the following.

Theorem 3.2 A trans-Sasakian manifold admits a proper concircular tensor field.

Where T is a conformally flat manifold M n (whose dimension is a grater than n) admits a proper concircular tensor field, then the manifold is a sub-projective manifold. Since the trans-Sasakian manifold M n admits proper concircular tensor field, namely the tensor fieldU, I can state as follows:

Theorem 3.3 A conformally flat trans-Sasakian manifold Mⁿ, is a sub-projective manifold in the sense of Kagan.

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